

<p><b>1(i)</b></p>	<p>Total has Poisson distribution with mean  <math>\lambda = 0.21 \times 5 + 0.24 \times 5 = 2.25</math></p> <p><math>P(\geq 2) = 1 - e^{-\lambda}(1+\lambda)</math>  <math>= 0.657</math></p>	<p>M1 A1</p> <p>M1 A1 <b>4</b></p>	<p>With <math>\times 5</math></p> <p><math>\lambda</math> or <math>1+\lambda</math> in brackets (their <math>\lambda</math>) Or interpolation from tables</p>
<p><b>(ii)</b></p>	<p>EITHER: Each length is a random sample OR: Flaws occur independently on the reels</p>	<p>B1 <b>1</b></p> <p><b>[5]</b></p>	<p>In context Accept randomly</p>
<p><b>2</b></p>	<p><math>H_0: \mu = (\text{or } \geq) 170, H_1: \mu &lt; 170</math>  <math>\bar{x} = 167.5</math>  <math>s^2 = 5.9</math></p> <p>EITHER: <math>(\alpha) (167.5 - 170) / \sqrt{(5.9/6)}</math>  <math>= -2.52(1)</math> Compare with <math>-2.015</math></p> <p>OR: <math>(\beta) 170 - t(5.9/6)</math>  <math>= 168.0</math> Compare 167.5 with CV and reject <math>H_0</math> There is sufficient evidence at the 5% significance level that the machine dispenses less than 170 ml on average.</p>	<p>B1 B1 B1</p> <p>M1 A1 M1</p> <p>M1 A1 M1</p> <p>A1</p> <p><b>[7]</b></p>	<p>For both hypotheses; accept words SR 2-tail test: B0B1B1M1A1M1A0 Max 5/7</p> <p>Standardise 167.5; + or - for M; /6 seen Explicitly Allow 2.571</p> <p>Finding critical value or region. With <math>t = 2.015</math> or 2.571 Explicitly. Allow correct use of <math> t </math> M0 if z used SR: B1 if no explicit comparison but conclusion "correct"</p>
<p><b>3(i)</b></p>	<p><math>H_0</math>: There is no association between the area in which a shopper lives and the day they shop  <math>(H_1</math>: All alternatives) E-Values 27.3 14.7 37.7 20.3  <math>\chi^2 = (4.3-0.5)^2(27.3^{-1}+37.7^{-1}+14.7^{-1}+20.3^{-1})</math>  <math>= 2.606</math> Compare with 2.706 Do not reject <math>H_0</math>. There is insufficient evidence of an association.</p> <p>SR: If <math>H_0</math> association, lose 1<sup>st</sup> B1 and last M1A1</p>	<p>B1</p> <p>M1 A1</p> <p>M1 ft A1 A1</p> <p>M1 A1 <b>8</b></p>	<p>SR difference in proportions B1 define and evaluate <math>p_1</math> and <math>p_2</math> with <math>H_0</math> B1 for <math>p=0.42</math> M1A1 for <math>z = \pm 1.827</math> or 1.835 (no pe) M1A0 Max 5/8</p> <p>At least one E value correct (M1) All correct(A1) At least one <math>\chi^2</math>, no or wrong cc, (M1FtE) All correct (A1); 2.606 or 2.61 (A1) Or use calculator (<math>p = 0.106</math>) SR: B1 if no explicit comparison, as Q2 SR: If <math>H_0</math> association, lose 1<sup>st</sup> B1 and last M1A1</p>
<p><b>(ii)</b></p>	<p>Conclusion the same since critical value &gt; 2.706 (and test statistic unchanged)</p>	<p>B1 <b>1</b></p> <p><b>[ 9]</b></p>	<p>OR from <math>z = \pm 2.17</math>, SR</p>

4(i)	$s^2 = (1183.65 - 246.6^2/70)/69$ Use $\bar{x} \pm zs/\sqrt{70}$ $s/\sqrt{70}$ 1.645 (3.10, 3.94)	M1 M1 A1 A1 A1	AEF Allow without ft or with $s^2$ ; with 70 Their s A0 if interval not indicated
(ii)	Change 90 to around 90	B1	Or equivalent
(iii)	$4(0.9)^3(0.1) + 0.9^4$  $= 0.9477$	M1  A1	Use of bino with $p=0.9$ or $0.1$ and 4 and Correct terms considered. art 0.948
5(i)	$e^{-2.25} - e^{-4}$ $\times 150$ $= 13.1$ Last: $150 - \text{sum} = 2.7$	M1 A1 A1 A1 ft	Or find last entry using $F(x)$  Or 2.7 if found first Or 13.1 any accuracy
(ii)	( $H_0$ : Data fits the model, $H_1$ : Data does not fit) Combine last two cells $\chi^2 = 7.8^2/33.2 + 11.6^2/61.6 + 7.4^2/39.4 + 11.2^2/15.8$ $= 13.3(46)$ Compare with 9.348 (or 11.14), reject $H_0$ (There is sufficient evidence at the $2\frac{1}{2}\%$ significance level that) the model is not a good fit	B1  M1*Dep A1 A1 M1  A1 ft Dep*	At least two correct All correct In range 13.2 to 13.5 SR: If last 2 cells are not combined B0M1A1A1(for 13.5) M1A1 If no explicit comparison B1 if conclusion follows
6(i)	Anxiety scores; have normal distributions; common variance; independent samples $H_0: \mu_E = \mu_C, H_1: \mu_E < \mu_C$ $s^2 = (1923.56 + 1147.58)/29 (= 105.9)$ $(t) = (32.16 - 38.21)/\sqrt{105.9(18^{-1} + 13^{-1})}$  $= -1.615$ $t_{crit} = -1.699$  Compare -1.615 with -1.699 and do not reject $H_0$ There is insufficient evidence at the 5% significance level to show that anxiety is reduced by listening to relaxation tapes	B2  B1 B1 M1 A1 A1 B1  M1  A1 ft	Context + 2 valid points B2 Context + 1VP, no context +2VP B1 Not in words  Allow 1 error; eg $s^2 =$ $1923.56/(17 \text{ or } 18)$ All correct + $47.5/(12 \text{ or } 13)$ Or + Or +; accept art $\pm 1.70$  Or +, +. M0 if $t$ not $\pm 1.699, \pm 2.045$  In context, not over-assertive OR Find CV or CR: B2B1B1; $C =$ or $\geq st, t = \pm 1.699$ or $\pm 2.015$ M1A1 $t = \pm 1.699$ B1; $G = 6.11(2)$ A1; $6.112 > 6.05$ and reject $H_0$ etc M1A1
(ii)	Sample sizes are too small (to appeal to CLT)	B1	

<p><b>7(i)</b></p>	<p>Use <math>\sum F + \sum M \sim N(\mu, \sigma^2)</math>  <math>\mu = 1104.9</math>  <math>\sigma^2 = 6 \times 9.3^2 + 9 \times 8.5^2</math>  <math>= 1169.2</math>  <math>P(&gt; 1150) = 1 - \Phi\left(\frac{1150 - 1104.9}{\sqrt{1169.2}}\right)</math>  <math>= 0.0937</math></p>	<p>M1 A1 M1 A1 M1 A1</p>	<p>Sum of indep normal variables is normal</p> <p>Standardise, correct tail. M0 <math>\sigma/\sqrt{15}</math> Accept .094</p>
<p><b>(ii)</b></p>	<p>If unknown M, prob <math>\frac{1}{2}</math>, 6F and 9M as before.          If unknown W, prob <math>\frac{1}{2}</math>, 7W and 8M          Having <math>N(1093.3, 1183.4)</math>  <math>P(&gt; 1150) = 1 - \Phi(1.648) = 0.0497</math>  <math>P = \frac{1}{2} \times 0.0936 + \frac{1}{2} \times 0.0497</math>  <math>= 0.07165</math></p>	<p>M1  B1 B1  A1 M1 A1</p>	<p>Considering two cases</p> <p>Mean and variance</p> <p>Use of <math>\frac{1}{2}</math> ART 0.072</p>
<p><b>8(i)</b></p>	<p><math>X = \frac{1}{4} S^2</math></p> $F(s) = \int_1^s \frac{8}{3s^3} ds = \left[ -\frac{4}{3s^2} \right]_1^s$ $= \frac{4}{3} (1 - 1/s^2)$ <p><math>G(x) = P(X \leq x) = P(S \leq 2\sqrt{x})</math>  <math>= F(2\sqrt{x})</math></p> $= \frac{4}{3} - \frac{1}{3x}$ $g(x) = \begin{cases} \frac{1}{3x^2} & \frac{1}{4} \leq x \leq 1, \\ 0 & \text{otherwise.} \end{cases}$	<p>B1  M1  A1 M1  A1 ft  M1 B1</p>	<p>Ignore range here</p> <p>SR: B1 for <math>G(x) = F(2\sqrt{x})</math> without justification and with correct result ft F</p> <p>For <math>G'(a)</math> For range</p>
<p><b>(ii)</b></p>	<p>EITHER: <math>G(m) = \frac{1}{2}</math>  <math>\Rightarrow \frac{4}{3} - \frac{1}{3m} = \frac{1}{2}</math>  <math>\Rightarrow m = \frac{2}{5}</math></p> <p>OR: <math>\int_{1/4}^m \frac{1}{3x^2} dx = \frac{1}{2}</math>  <math>\Rightarrow \left[ -\frac{1}{3x} \right]_{1/4}^m = \frac{1}{2}</math>  <math>\Rightarrow m = \frac{2}{5}</math></p>	<p>M1  A1 ft A1  M1  A1 A1</p>	<p>ft <math>G(x)</math> in (i)</p> <p>CAO</p> <p>Allow wrong <math>\frac{1}{4}</math></p> <p>Allow wrong <math>\frac{1}{4}</math></p> <p>CAO</p>
		<p><b>6</b> <b>[12]</b></p>	
		<p><b>7</b></p>	
		<p><b>3</b> <b>[10]</b></p>	